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Covalency and vibronic couplings make a nonmagnetic j = 3/2ion magnetic

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For $4d^1$ and $5d^1$ spin—orbit-coupled electron configurations, the notion of nonmagnetic i=3/2 quartet ground state discussed in classical textbooks is at odds with the observed variety of magnetic properties. Here we throw fresh light on the electronic structure of $4d^1$ and $5d^1$ ions in molybdenum- and osmium-based double-perovskite systems and reveal different kinds of on-site many-body physics in the two families of compounds: although the sizable magnetic moments and q-factors measured experimentally are due to both metal d-ligand p hybridisation and dynamic Jahn-Teller interactions for 4d electrons, it is essentially d-p covalency for the 5d¹ configuration. These results highlight the subtle interplay of spin-orbit interactions, covalency and electron-lattice couplings as the major factor in deciding the nature of the magnetic ground states of 4d and 5d quantum materials. Cation charge imbalance in the double-perovskite structure is further shown to allow a fine tuning of the gap between the t_{2q} and e_q levels, an effect of much potential in the context of orbital engineering in oxide electronics.

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INTRODUCTION

A defining feature of *d*-electron systems is the presence of sizable electron correlations, also referred to as Mott-Hubbard physics. The latter has been traditionally associated with first-series (3d) transition-metal (TM) oxides. But recently one more ingredient entered the TM oxide 'Mottness' paradigm—large spin-orbit couplings (SOCs) in 4d and 5d quantum materials. 1,2 It turns out that for specific t_{2a} -shell electron configurations, a strong SOC can effectively augment the effect of Hubbard correlations: 1 although the 4d and 5d orbitals are relatively extended objects and the Coulomb repulsive interactions are weakened as compared with the more compact 3d states, the spin-orbit-induced level splittings can become large enough to break apart the 'nonrelativistic' t_{2q} bands into sets of well-separated, significantly narrower subbands for which even a modest Hubbard *U* acting on the respective Wannier orbitals can then open up a finite Mott-Hubbard-like gap.¹ On top of that, SOC additionally reshuffles the intersite superexchange.3 The surprisingly large anisotropic magnetic interactions $\bar{\text{th}}\text{at}$ come into play via the strong SOCs in iridates,^{3–8} e.g., are responsible for an exotic assortment of novel magnetic ground states and excitations.^{2,3,9}

For large t_{2g} – e_g splittings, the spin–orbit-coupled t_{2g}^1 and t_{2g}^5 electron configurations can be in first approximation viewed as 'complementary': in the simplest picture, the *d*-shell manifold can be shrunk to the set of j = 1/2 and j = 3/2 relativistic levels, with a j=3/2 ground state for the TM t_{2g}^1 configuration and a j=1/2 ground state for t_{2g}^5 . t_{2g}^{10-12} Although strongly spin—orbit-coupled t_{2g}^5 oxides and halides—iridates, rhodates and ruthenates, in particular—have generated substantial experimental and theoretical investigations in recent years, much of the properties of 5d and 4d t_{2g}^1 systems remain to large extent unexplored. From textbook arguments, $^{10-12}$ the t_{2g}^1 j = 3/2 quadruplet should

be characterised by a vanishing magnetic moment in cubic

symmetry, due to perfect cancellation of the spin and angular momentum contributions. But this assertion leaves unexplained the wide variety of magnetic properties recently found in 4d¹ and $5d^1$ cubic oxide compounds. ^{13–20} Ba₂YMoO₆, e.g., develops no magnetic order despite a Curie–Weiss temperature of ≈ - 200 K (refs 13,14) and features complex magnetic dynamics that persists down to the mK range, possibly due to either a valence-bondglass¹⁵ or spin-liquid¹⁶ ground state. Also, Ba₂NaOsO₆ displays an antiferromagnetic Curie-Weiss temperature 18,19 but orders ferromagnetically below 7 K (ref. 20), whereas Ba₂LiOsO₆ is a spin-flop antiferromagnet.20

Here we carry out a detailed ab initio investigation of the Mo⁵⁺ $4d^{1}$ and Os^{7+} $5d^{1}$ relativistic electronic structure in the doubleperovskite compounds Ba₂YMoO₆, Ba₂LiOsO₆ and Ba₂NaOsO₆. In addition to providing reliable results for the energy scale of the dlevel splittings, $t_{2g} - e_g$ and induced by SOC within the t_{2g}^1 manifold, we analyse the role of TM d-O p orbital mixing plus the strength of electron-lattice couplings. It is found that strong metal d - Op hybridisation generates a finite magnetic moment even for perfectly cubic environment around the TM site, providing ab initio support to the phenomenological covalency factor introduced in this context by Stevens.²¹ The TM d^1 magnetic moment is further enhanced by tetragonal distortions, against which the octahedral oxygen cage is unstable. According to our results, such Jahn-Teller (JT) effects are particularly strong for the Mo 4d¹ ions in Ba₂YMoO₆. Although additional investigations are needed for clarifying the role of intersite cooperative couplings, 22,23 our calculations emphasise the high sensitivity of the effective magnetic moments to both metal-ligand covalency effects and local JT physics. The material dependence for the ratio among the strengths of the spin-orbit interaction, the JT coupling parameter and the effective covalency factor that we compute

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here provide a solid basis for future studies addressing the role of intersite interactions on the double-perovskite fcc lattice.

RESULTS

Quantum chemistry calculations were first performed to resolve the essential features of the electronic structure of the cubic lattice configuration, without accounting for electron–lattice couplings (see Materials and methods for computational details and Figure 1 for a sketch of a three-dimensional double-perovskite crystal). Results for the splitting between the Mo⁵⁺ t_{2g}^1 j = 3/2 and j = 1/2 spin–orbit states, $\Delta_{3/2 \rightarrow 1/2}$, are provided in Table 1 at two levels of approximation, i.e., multiconfiguration complete-active-space self-consistent field (CASSCF) and multireference configuration interaction (MRCI) with single and double excitations on top of the CASSCF wave function. And the splitting $\Delta_{3/2 \rightarrow 1/2}$, the strength of the SOC parameter can be easily derived as $\lambda = \frac{2}{3}\Delta_{3/2 \rightarrow 1/2}^{CASSCF}$. The resulting λ of 89 meV is somewhat smaller than earlier estimates of 99 meV for Mo⁵⁺ impurities in SrTiO₃. A most interesting finding, however, is that despite the cubic environment the quantum chemistry calculations yield

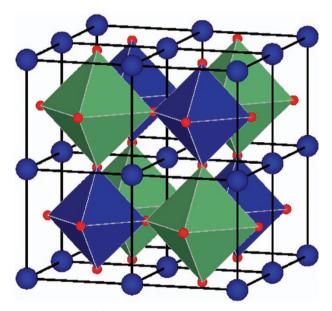


Figure 1. Sketch of the atomic positions in a cubic double-perovskite compound, $Ba_2BB'O_6$. B stands here for Y, Na or Li (site at the centre of a dark-blue octahedron); B' is either Mo or Os (site at the centre of a light-green octahedron). O ions are shown as small red spheres, whereas the Ba sites are the larger blue spheres.

Table 1. Mo⁵⁺ 4*d*-shell splittings (j = 3/2 to j = 1/2 and $t_{2g} - e_g$) and 'static' g_{\parallel} factor in cubic Ba₂YMoO₆

4d¹ electronic structure	CASSCF	MRCI
$\Delta_{3/2 \rightarrow 1/2}$ (eV)	0.133	0.130
$\Delta_{t_{2g} o e_g}$ (eV) $g_{ }$	4.80 0.18	4.51 0.20

Abbreviations: CASSCF, complete-active-space self-consistent field; MRCI, multireference configuration interaction; SOC, spin–orbit coupling. Three orbitals (4d t_{2g}) were active in the CASSCF calculation for $\Delta_{3/2 \rightarrow 1/2r}$ whereas five orbitals were active in the calculations for g_{\parallel} and $\Delta_{t2g \rightarrow eg}$ (sans SOC for the latter).

nonvanishing magnetic moment and a finite g-factor. This obviously does not fit the nonmagnetic j=3/2 quartet ground state assumed to arise in standard textbooks on crystal-field theory^{11,12} from exact cancellation between the spin and the orbital moments.

At a qualitative level, it has been argued by Stevens²¹ that finite g-factor values can in fact occur for j = 3/2 ions due to TM-O covalency on the TM O₆ octahedron. For better insight into the nature of such effects, we therefore performed a simple numerical experiment in which the six ligands coordinating the reference Mo^{5+} $4d^1$ ion are replaced by -2 point charges with no atomic basis functions. In that additional set of computations the magnetic moment and the *q*-factor do vanish, in agreement with the purely ionic picture of Kotani, Abragam and Bleaney. 10,11 This shows that one tuning knob for switching magnetism on is indeed the TM 4d - O 2p orbital hybridisation. The latter is strong for high ionisation states such as Mo⁵⁺ (as the tails of the 4*d*-like valence orbitals indicate in the case the nearest-neighbor ligands are provided with atomic basis sets, see Figure 2a), gives rise to partial quenching of the orbital moment and makes that the exact cancellation between the spin and the orbital moments no longer holds.

We find that this effect is even stronger for the formally 7+ Os ion in $\text{Ba}_2\text{LiOsO}_6$ and $\text{Ba}_2\text{NaOsO}_6$. As shown in Table 2, g-factors as large as 0.4 are computed in this case. The quantum chemistry results also allow us to estimate the strength of the effective Os $^{7+}$ SOC constant, with $\lambda = \frac{2}{3}\Delta_{3/2-1/2}^{\text{CASSCF}} = 387$ meV, lower than $\lambda = 468$ meV in tetravalent $5d^5$ iridates. 26

As the t_{2g}^1 electron configuration is susceptible to JT effects, we carried out further investigations on the stability of an ideal TM O_6 octahedron against tetragonal (z axis) distortions. A total-energy profile for specified geometric configurations is provided in Figure 2c for an embedded Mo O_6 octahedron. It is seen that the minimum corresponds to $\sim 3\%$ tetragonal compression, as compared with the cubic octahedron of the Fm3m crystalline structure. As expected, the magnetic moment rapidly increases in the presence of distortions, as illustrated in Table 3 and Figure 2d.

Depending on further details related to the strength of the intersite couplings among 'JT centres', static deformations away from cubic symmetry may be realised in some systems, as observed for example in the Re^{6+} $5d^{1}$ double-perovskite Sr₂MgReO₆ (ref. 27) and rare-earth molibdates.^{28,29} If the local JT couplings and intersite interactions are relatively weak, one may be left on the other hand in a dynamic JT regime, as earlier pointed out for the particular t_{2g}^1 configuration by, e.g., Kahn and Kettle.³⁰ The relevant vibrational modes that couple to the ${}^{2}T_{2q}(t_{2q}^{1})$ electronic term are those of E_{q} symmetry ((3 $z^{2}-r^{2}$)and $(x^2 - y^2)$ -like). From the quantum chemistry calculations, we find that the potential-energy well is significantly shallower for these normal coordinates, as compared with z axis-only compression. The value we computed for the Mo⁵⁺ ion in Ba₂YMoO₆, ≈40 meV, is comparable to the estimate made in the 1970s for Mo^{5+} t_{2q}^1 impurity ions within the SrTiO₃ matrix, \approx 60 meV. ²⁵ For the osmates, the depth of this potential well is much reduced, with $E_{\rm IT}$ values in the range of 10–15 meV by spin-orbit MRCI calculations

The vibronic model of Kahn and Kettle³⁰ provides specific expressions for the g-factors. In particular, g_{\parallel} can be parametrised as³⁰

$$g_{\parallel} = 2(1 - k_{\text{cov}} k_{\text{vib}}), \tag{1}$$

where k_{cov} is Stevens' covalency factor²¹ and

$$k_{\text{vib}} = \exp[-x/(1+\rho)]. \tag{2}$$

The parameters x and ρ are defined as $x=3E_{JT}/2\overline{h}\omega$ and $\rho=3\lambda/2\overline{h}\omega$, where $\overline{h}\omega$ is the E_g -mode vibrational energy and $g_{\perp}=0$ by symmetry. Recent infrared transmission spectra

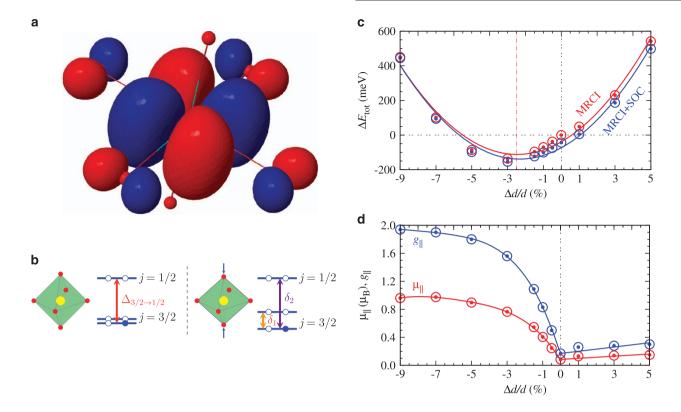


Figure 2. (a) Mo $4d t_{2g}$ charge distribution as obtained by CASSCF calculations. The tails at the nearest-neighbor O sites have substantial weight. (b) TM t_{2a} splittings in cubic (left) and tetragonal (right) symmetry; $\delta_1 = 0$ and $\delta_2 = \Delta_{3/2 \to 1/2}$ for cubic octahedra. (c) Ground-state energy as function of z axis tetragonal distortion, MRCI results both with and without spin-orbit coupling. (d) Variation of the Mo $4d^1$ magnetic moment (μ_{\parallel}) and g-factor (g_{\parallel}) with the amount of z axis tetragonal distortion, MRCI results including spin-orbit interactions.

Table 2. Os⁷⁺ 5*d*-shell splittings (j = 3/2 to j = 1/2 and $t_{2q} - e_q$) and 'static' q_{II} factors in cubic Ba₂LiOsO₆ and Ba₂NaOsO₆

5d¹ electronic structure	CASSCF	MRCI
Ba_2LiOsO_6 $\Delta_{3/2 \rightarrow 1/2}$ $\Delta_{t_{2g} \rightarrow e_g}$ g_{\parallel}	0.58 6.17 (6.44) 0.39	0.56 5.95 (6.21) 0.40
Ba_2NaOsO_6 $\Delta_{3/2 \rightarrow 1/2}$ $\Delta_{t_{2g} \rightarrow e_g}$ $g_{ }$	0.58 6.41 (6.68) 0.31	0.57 6.19 (6.45) 0.40

Abbreviations: CASSCF, complete-active-space self-consistent field; MRCI, multireference configuration interaction; SOC, spin-orbit coupling. Only the 5d t_{2a} orbitals were active in the CASSCF calculation for $\Delta_{3/2 \to 1/2}$; all five 5d orbitals were active in the calculations for g_{\parallel} and $\Delta_{t_{2q} \to e_q}$. For the latter, values including SOC are provided within parantheses. All energies in eV.

indicate that $\overline{h}\omega \approx$ 560 cm⁻¹ \approx 70 meV for the bond-stretching phonons. The effective parameter $k_{\rm cov}$ we can easily evaluate from the static g_{\parallel} values obtained in the MRCI spin-orbit treatment (Tables 1 and 2) if vibronic interactions are neglected $(k_{\text{vib}} = 1 \text{ for 'frozen' cubic octahedra})$, with $k_{\text{cov}} \equiv 1 - g_{\parallel}^{\text{MRCI}}/2$. This yields covalency reduction factors of 0.90 for Ba₂YMoO₆ and 0.80 for the osmates.

Table 3. Mo⁵⁺ t_{2a}^1 electronic structure with 'static' tetragonal squeezing of the reference MoO₆ octahedron

MoO ₆ flattening	0.5%	1.5%	3%	5%
$\Delta_{t_{2a}}$	0.02	0.07	0.15	0.27
$egin{array}{c} \Delta_{t_{2g}} \ \delta_1 \ \delta_2 \end{array}$	0.02	0.05	0.12	0.24
δ_2	0.14	0.17	0.23	0.33
$\mu_{ } (\mu_{B})$	0.24	0.55	0.75	0.89
$g_{\parallel} (k_{\text{vib}} = 1)$	0.50	1.09	1.55	1.80

Abbreviations: CASSCF, complete-active-space self-consistent field; MRCI, multireference configuration interaction; SOC, spin-orbit coupling. Only the t_{2g}^1 configuration was considered in the reference CASSCF. $\Delta_{t_{2g}}$ is t_{2g} tetragonal splitting without SOC, δ_1 and δ_2 are excitation energies within the t_{2g}^1 manifold with SOC accounted for $(\delta_1 = 0 \text{ and } \delta_2 = \Delta_{3/2 \to 1/2} \text{ for cubic}$ octahedra, see Figure 2b). MRCI results, all energies in eV.

Table 4. TM q_{\parallel} factors using the Kahn-Kettle vibronic model³⁰ and ab initio estimates for λ , k_{cov} and E_{IT}

	E_{JT}	x	ρ	k_{vib}	k _{cov}	gп
Mo ⁵⁺ 4d ¹ , Ba ₂ YMoO ₆	40	0.86	1.90	0.74	0.90	0.66
Os ⁷⁺ 5d ¹ , Ba ₂ LiOsO ₆	10	0.21	8.29	0.98	0.80	0.44
Os ⁷⁺ 5d ¹ , Ba ₂ NaOsO ₆	15	0.32	8.29	0.97	0.80	0.45

 $x=3E_{\rm JT}/2\overline{h}\omega,~~
ho=3\lambda/2\overline{h}\omega,~~\overline{h}\omega$ is set to 70 meV (refs 17,31) and $q_{||} = 2(1 - k_{cov}k_{vib}).$

Estimates for g_{\parallel} are provided in Table 4, using the Kahn–Kettle vibronic model and the quantum chemistry results for λ , k_{cov} and E_{JT} . It is seen that a large ρ/x ratio (i.e., large λ/E_{JT}) makes that g_{\parallel} is generated mostly through covalency effects in the osmates, with minor contributions from vibronic couplings. On the other hand, the small ρ/x ratio in Ba₂YMoO₆ gives rise to a strong enhancement of g_{\parallel} through vibronic effects, with a factor of nearly 4 between $(1-k_{\text{cov}}k_{\text{vib}})$ and $(1-k_{\text{cov}})$. This way, the interesting situation arises that the TM magnetic moment is mainly due to vibronic effects in Ba₂YMoO₆ and predominantly to strong covalency in Ba₂LiOsO₆ and Ba₂NaOsO₆.

DISCUSSION

Experimentally, the measured magnetic moments are indeed significantly smaller in Ba₂LiOsO₆ and Ba₂NaOsO₆ (refs 19,20) as compared with Ba₂YMoO₆ (refs 13,14,17,25). With regard to the estimates we make here for g_{\parallel} , possible sources of errors concern the accuracy of the calculated E_{IT} when using the experimental crystal structure as reference and correlation and polarisation effects beyond a single TM O_6 octahedron. The latter effects would only increase E_{IT} . With respect to the former aspect, it is known that by advanced quantum chemistry calculations, the lattice constants of TM oxides can be computed with deviations of < 0.5% from the measured values, 32 which implies rather small corrections to E_{JT} . Interestingly, recent findings of additional phonon modes at low temperatures 17 indicate static distortions of the MoO₆ octahedra in Ba₂YMoO₆ and indeed a rather large $E_{\rm JT}$. More detailed investigations on this matter are left for future work. Valuable experimental data that can be directly compared with our calculations would be the results of electron spin resonance measurements of the q-factors.

It is also worth pointing out that using the Kahn–Kettle model even a E_{JT} of 75 meV, five to seven times larger than the values computed by MRCI for the osmates (Table 4), still yields a rather moderate g_{\parallel} factor of 0.65 for the Os $5d^1$ ion. Such g_{\parallel} factors of 0.4–0.6 compare quite well with the low-temperature magnetic moment derived from magnetisation and muon spin relaxation measurements on Ba₂NaOsO₆, \approx 0.2 $\mu_{\rm B}$. For the Mo $4d^1$ ion in Ba₂YMoO₆, the computed g_{\parallel} factor is much more sensitive to variations of E_{JT} —increasing E_{JT} from, e.g., 40–200 meV enhances g_{\parallel} of Equation (1) from \approx 0.6 to \approx 1.6.

One other remarkable prediction of Kahn and Kettle³⁰ is that the splitting of the j=3/2 and j=1/2 states is increased through vibronic couplings, by a factor

$$\gamma = 1 + x \frac{3 + \rho}{3(\rho^2 - 1)}. (3)$$

This effect turns out to be small in the osmates, given the small x and large ρ in those compounds. But we compute a strong modification of the j=3/2 to j=1/2 excitation energy for Ba₂YMoO₆, from ~0.13 eV in the absence of vibronic interactions (Table 1) to ≈0.20 eV with JT effects included (E_{JT} = 40 meV). Experimentally, the situation can be clarified by direct resonant inelastic X-ray scattering (RIXS) measurements on Ba₂YMoO₆. High-resolution RIXS measurements could also address the occurrence of static distortions at low temperatures, suggested for Ba₂YMoO₆ on the basis of extra phonon modes in the low-T infrared transmission spectra¹⁷ and for Ba₂NaOsO₆ from the integrated entropy through the magnetic phase transition at \sim 7 $m K.^{19}$ According to the MRCI data in Table 3, a reduction by 0.5-1.5% of the interatomic distances on one set of O-Mo-O links already gives a splitting of 20-50 meV of the low-lying spin-orbit states. Splittings of this size should be accessible with lastgeneration RIXS apparatus.

Also of interest is an experimental confirmation of the unusually large $t_{2g} - e_g$ gap we predict in the double-perovskite heptavalent osmates, \gtrsim 6 eV (Table 2). According to the results of additional

computations we carried out, the source of this exceptional d-level splitting is the stabilisation of the Os t_{2a} states due to the large effective charge (formally 7+) at the nearest-neighbor Os sites. The latter are situated on the axes along which the lobes of the t_{2a} orbitals are oriented; in contrast, the lobes of the e_a functions point towards the monovalent species (Li¹⁺ or Na¹⁺). For example, test CASSCF calculations in which the size of the point charges placed at the 12 Os and 6 alkaline-ion nearest-neighbor sites are modified from the formal ionic values 7+ and 1+ (12×7) $+6\times1=90$) to 5+ and 5+ $(12\times5+6\times5=90)$ show a reduction of about 2 eV of the $t_{2a} - e_a$ level splitting. Similar effects, with relative shifts and even inversion of the d-electron energy levels due to charge imbalance at nearby cation sites, were recently evidenced in Sr_2RhO_4 and Sr_2lrO_4 , 8,26 the rare-earth 227 iridates $R_2lr_2O_7$ (ref. 34) and $Cd_2Os_2O_7$. The mechanism has not been thoroughly explored so far experimentally but seems to hold much potential in the context of orbital engineering in TM compounds.

To summarise, it is well known that nominal orbital degeneracy gives rise in 3d TM oxides to subtle couplings between the electronic and lattice degrees of freedom and very rich physics. Here we resolve the effect of electron-lattice interactions on the magnetic properties of heavier, 4d and 5d TM ions with a formally degenerate t_{2q}^1 electron configuration in the double-perovskite materials Ba₂YMoO₆, Ba₂LiOsO₆ and Ba₂NaOsO₆. In particular, using advanced quantum chemistry electronic-structure calculations, we reconcile the notion of a nonmagnetic spin-orbitcoupled $t_{2g}^1 j = 3/2$ ground state put forward by Kotani, Abragam, Bleaney and others^{10–12} with the variety of magnetic properties recently observed in $4d^1$ and $5d^1$ double perovskites. Our analysis shows that the sizable magnetic moments and q-factors found experimentally are due to strong TM d-ligand p hybridisation and dynamic JT effects, providing new perspectives on the interplay between metal-ligand interactions and SOCs in TM oxides. It also highlights the proper theoretical frame for addressing the remarkably rich magnetic properties of d^1 double perovskites^{2,15,16,19,20} in particular. Over the past two decades, vibronic couplings have unjustifiably received low attention in the case of these intriguing materials.

MATERIALS AND METHODS

All *ab initio* calculations were carried out with the quantum chemistry package Molpro.³⁶ Crystallographic data as derived in ref. 14 for Ba₂YMoO₆ and in ref. 18 for Ba₂LiOsO₆ and Ba₂NaOsO₆ were employed.

We used effective core potentials, valence basis functions of triple-zeta quality and two *f* polarisation functions for the reference Mo/Os ions^{37,38} for which the *d*-shell excitations are explicitly computed. Allelectron triple-zeta basis sets supplemented with two *d* polarisation functions³⁹ were applied for each of the six adjacent O ligands. The eight Ba nearest neighbours were in each case modelled by Ba²⁺ 'total-ion' pseudopotentials supplemented with a single *s* function.⁴⁰ For Ba₂YMoO₆, the six nearby Y sites were described by effective core potentials and valence basis functions of double-zeta quality.³⁷ In Ba₂LiOsO₆ and Ba₂NaOsO₆, we employed total-ion pseudopotentials for the six nearest Li and Na cations and sets of one *s* and one *p* functions.⁴¹ The farther solid-state surroundings enter the quantum chemistry calculations at the level of a Madelung ionic potential. How the complexity and accuracy of quantum chemistry calculations for an infinite solid can be systematically increased is addressed in, e.g., refs 32,33,42,43.

For the CASSCF calculations of the d-shell splittings, we used active spaces of either three (t_{2g}) or five (t_{2g}) plus $e_g)$ orbitals. The CASSCF optimisations were carried out for an average of either the ${}^2T_{2g}$ (t_{2g}^1) or ${}^2T_{2g}(t_{2g}^1) + {}^2E_{2g}(e_g^1)$ eigenfunctions of the scalar relativistic Hamiltonian. All O 2p and Mo/Os 4d/5d electrons on the reference TM O₆ octahedron were correlated in the MRCI treatment. The latter was performed with single and double substitutions with respect to the CASSCF reference, as described in refs 44,45. The spin–orbit treatment was carried out according to the procedure described in ref. 46.

The q-factors were computed following a scheme proposed by Bolvin⁴⁷ and Vancoillie. 48 For a Kramers-doublet ground state $\{\psi, \overline{\psi}\}$, the Abragam– Bleaney tensor¹¹ $G = gg^T$ can be expressed in matrix form as

$$G_{kl} = 2 \sum_{u,v=\psi,\overline{\psi}} \langle u | \hat{L}_k + g_e \hat{S}_k | v \rangle \langle v | \hat{L}_l + g_e \hat{S}_l | u \rangle$$

$$= \sum_{m=v,v} \left(\Lambda_{km} + g_e \sum_{km} \right) \left(\Lambda_{lm} + g_e \sum_{lm} \right), \tag{4}$$

where q_e is the free-electron q-factor and

$$\begin{split} &\Lambda_{kx} = 2Re\big[\langle\overline{\psi}|\hat{L}_{k}|\psi\rangle\big], \quad \sum_{kx} = 2Re\big[\langle\overline{\psi}|\hat{S}_{k}|\psi\rangle\big], \\ &\Lambda_{ky} = 2Im\big[\langle\overline{\psi}|\hat{L}_{k}|\psi\rangle\big], \quad \sum_{ky} = 2Im\big[\langle\overline{\psi}|\hat{S}_{k}|\psi\rangle\big], \\ &\Lambda_{kz} = 2\big[\langle\psi|\hat{L}_{k}|\psi\rangle\big], \quad \sum_{kz} = 2\big[\langle\psi|\hat{S}_{k}|\psi\rangle\big]. \end{split} \tag{5}$$

The matrix elements of \hat{L} were extracted from the Molpro outputs, whereas the matrix elements of \hat{S} were derived using the conventional expressions for the generalised Pauli matrices:

$$\begin{aligned}
(\hat{S}_z)_{MM'} &= M\delta_{MM'}, \\
(\hat{S}_x)_{MM'} &= \frac{1}{2}\sqrt{(S+M)(S-M+1)}\delta_{M-1,M'} \\
&+ \frac{1}{2}\sqrt{(S-M)(S+M+1)}\delta_{M+1,M'}, \\
(\hat{S}_y)_{MM'} &= -\frac{i}{2}\sqrt{(S+M)(S-M+1)}\delta_{M-1,M'} \\
&+ \frac{i}{2}\sqrt{(S-M)(S+M+1)}\delta_{M+1,M'}.
\end{aligned} (6)$$

The *q*-factors were calculated as the positive square roots of the three eigenvalues of G.

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CONTRIBUTIONS

L.X. carried out the ab initio quantum chemistry calculations, with assistance from N. A.B., A.P., P.F. and L.H. The mapping of the ab initio data onto the effective vibronic model was performed by L.X., L.H. and P.F. L.H., P.F. and J.vdB. designed the project. L. X. and L.H. wrote the paper, with contributions from all other coauthors.

COMPETING INTERESTS

The authors declare no conflict of interest.

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