Editors' Suggestion

Spin-glass state and reversed magnetic anisotropy induced by Cr doping in the Kitaev magnet α-RuCl₃

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(Received 1 March 2019; published 6 June 2019)

Magnetic properties of the substitution series $Ru_{1-x}Cr_xCl_3$ were investigated to determine the evolution from the anisotropic Kitaev magnet α -RuCl₃ with $J_{\text{eff}} = 1/2$ magnetic Ru³⁺ ions to the isotropic Heisenberg magnet $CrCl_3$ with S = 3/2 magnetic Cr^{3+} ions. Magnetization measurements on single crystals revealed a reversal of the magnetic anisotropy under doping, which we argue to arise from the competition between anisotropic Kitaev and off-diagonal interactions on the Ru-Ru links and approximately isotropic Cr-Ru and isotropic Cr-Cr interactions. In addition, combined magnetization, ac susceptibility, and specific-heat measurements clearly show the destabilization of the long-range magnetic order of α -RuCl₃ in favor of a spin-glass state of Ru_{1-x}Cr_xCl₃ for a low doping of x = 0.1. The corresponding freezing temperature as a function of Cr content shows a broad maximum around x = 0.45.

DOI: 10.1103/PhysRevB.99.214410

I. INTRODUCTION

The Kitaev model on a honeycomb lattice realizes a topological spin liquid in two space dimensions with fractionalized Majorana-fermion excitations [1-3]. The model is constructed from bond-dependent Ising interactions K between nearestneighbor moments which induce strong exchange frustration. Crucial ingredients for realizing the Kitaev model in materials are strong spin-orbit coupling combined with cancellation tendencies between multiple exchange paths [4]. The presence of dominant Kitaev interactions was first suggested for honeycomb iridates [5] and later for α -RuCl₃, based on an unusual magnetic excitation spectrum [6,7], strong magnetic anisotropy [8], and electronic-structure calculations [9,10].

 α -RuCl₃ is a $J_{\text{eff}} = 1/2$ Mott insulator with a layered structure of edge-sharing (RuCl₆) octahedra forming a honeycomb lattice [11]. These van-der-Waals-bonded honeycomb layers are arranged in a monoclinic unit cell at room temperature (space group C2/m) [12]; however, the stacking of these layers may be inhomogeneous depending on the crystal quality [13]. Apart from a dominant Kitaev exchange interaction, additional magnetic interactions such as nearest- and nextnearest-neighbor Heisenberg interactions J and symmetric off-diagonal couplings Γ have to be considered in a minimal

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model to describe the physics of α -RuCl₃ [9,10,14,15]. Due to these additional terms in the Hamiltonian, α -RuCl₃ orders in an antiferromagnetic zigzag state at low temperature [12,13]. Two magnetic transitions were identified at $T_N \simeq 7$ K and $T_N \simeq 13$ K in Ref. [13], based on a C^2/m space group, with magnetic wave vectors (0, 1, 1/3) (ABC stacking) and (0, 1,1/2) (AB stacking), respectively. These orders can coexist in the same single crystal, which may contain several magnetic domains [8,13,16]. Although α -RuCl₃ has an antiferromagnetic ground state, it is considered as a proximate Kitaev system since signatures of Majorana fermions were recently reported in the paramagnetic state above T_N [6,17–19]. Furthermore, magnetic fields of about $\mu_0 H_c \simeq 7$ – 8 T suppress long-range magnetic order toward a quantum paramagnetic state which has been proposed to realize a quantum spin liquid [8,20–25]. In addition, recent high-pressure experiments showed that a tiny hydrostatic pressure of $p \subseteq$ 0.2 GPa induces a structural transition toward a valence-bond crystal [26,27]. Chemical substitution of Cl by Br leads to an expansion of the honeycomb lattice and a concomitant increase of the Néel temperature [28].

A viable route to tune the magnetic properties of Kitaev magnets and in particular of α-RuCl₃ is chemical substitution on the magnetic-ion site. This has been discussed in several theoretical studies for the pure Kitaev limit [29-33], where it was shown that the spin-liquid state is relatively robust under doping and that the Majorana fermions can screen magnetic impurities resulting in a Kondo effect. Experimental studies on honeycomb iridates showed that the substitution of Ir⁴⁺ by nonmagnetic ions, such as Ti⁴⁺ in Li₂Ir_{1-x}Ti_xO₃ and Na₂Ir_{1-x}Ti_xO₃, and also by strongly spin-orbit-coupled magnetic ions, e.g., Ru⁴⁺ in Na₂Ir_{1-x}Ru_xO₃, changes the

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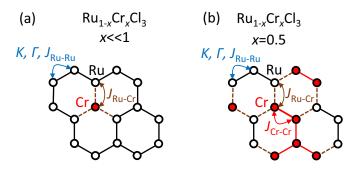


FIG. 1. (a) Schematic view of the honeycomb layer built by the Ru and Cr ions in $Ru_{1-x}Cr_xCl_3$ in the $x \ll 1$ limit. The red and white balls represent the Cr and Ru sites, respectively. The black, brown, and red nearest-neighbor links correspond to Ru-Ru, Ru-Cr, and Cr-Cr nearest-neighbor links, respectively, together with the arrows indicating the dominant magnetic nearest-neighbor interactions. (b) Same for x = 0.5.

antiferromagnetic zigzag state into a spin-glass state [34,35]. Via Monte Carlo calculations on the Kitaev-Heisenberg model this formation of a spin-glass state under the substitution of the magnetic ion by a nonmagnetic ion [36] or by magnetic ions [37] has successfully been rationalized. On the other hand, in α -RuCl₃ the substitution by nonmagnetic Ir³⁺ did not lead to a spin-glass state in Ru_{1-x}Ir_xCl₃. Instead, the Néel temperatures corresponding to the regions of ABC and of AB stacking domains in Ru_{1-x}Ir_xCl₃ both decrease continuously with the Ir content x and vanish around $x \simeq 0.11$ and $x \simeq 0.24$, respectively [38,39]. The nature of the quantum disordered state beyond $x \simeq 0.24$ is under debate, with a dilute spin liquid being proposed from inelastic neutron scattering experiments in Ref. [38].

In this paper we focus on the substitution of Ru³⁺ in α -RuCl₃ by magnetic Cr³⁺ ions. The possibility of crystal growth of Ru_{1-x}Cr_xCl₃ crystals with a homogeneous distribution of Ru and Cr on the same crystallographic site was previously reported [40,41]. The magnetic moment of the Cr site is not subject to strong spin-orbit coupling and can thus be considered as a spin-only moment S = 3/2. The honeycomb layer of Ru_{1-x}Cr_xCl₃ is represented in Fig. 1 together with the presumed main magnetic interactions. While the magnetic interactions on Ru-Ru nearest-neighbor links can be assumed to be the sum of Kitaev, Heisenberg, and off-diagonal interactions, the magnetic interactions on Cr-Cr nearest-neighbor links are expected to be of Heisenberg type. The nature of the magnetic interactions on the nearest-neighbor links Ru-Cr, however, remains to be determined. Thus, for low doping levels $x \ll 1$, the Ru_{1-x}Cr_xCl₃ series allows to study the role of magnetic impurities in a Kitaev magnet, while for higher doping levels the evolution from a frustrated Kitaev magnet to a non-frustrated Heisenberg magnet on a honeycomb lattice can be investigated.

The final member of the series, $CrCl_3$, crystallizes in the same monoclinic crystal structure as α -RuCl₃ [42]. It orders antiferromagnetically at $T_N = 14$ K with a ferromagnetic inplane alignment of the spins within the honeycomb layers and an antiparallel alignment of the spins for adjacent layers [43,44]. Further, a two-dimensional ferromagnetic ordering at

 $T_{\rm 2D} = 17$ K prior to the long-range antiferromagnetic ordering at 14 K was proposed from Faraday rotation and specific-heat measurements [44,45].

It is the purpose of this paper to discuss the magnetic properties of the complete $\mathrm{Ru}_{1-x}\mathrm{Cr}_x\mathrm{Cl}_3$ series based on magnetization, specific-heat, and ac susceptibility measurements. The combination of these thermodynamic probes allows us to construct the x-T phase diagram of $\mathrm{Ru}_{1-x}\mathrm{Cr}_x\mathrm{Cl}_3$, where the antiferromagnetic zigzag order is replaced by a spinglass state for $0.1 \lesssim x \lesssim 0.7$. Interestingly, the evolution of the magnetic anisotropy in the $\mathrm{Ru}_{1-x}\mathrm{Cr}_x\mathrm{Cl}_3$ series reveals a competition between anisotropic interactions on the Ru-Ru links and more isotropic interactions on Ru-Cr and Cr-Cr links. Notably, the substitution series $\mathrm{Ru}_{1-x}\mathrm{Cr}_x\mathrm{Cl}_3$ constitutes one of the rare cases with simultaneous tuning of frustration and disorder.

II. EXPERIMENTAL TECHNIQUES

The Ru_{1-x}Cr_xCl₃ single crystals were grown by a chemical vapor transport reaction in a two-zone furnace with a temperature gradient between 750°C and 650°C for 5 days. x-Ray diffraction, transmission electron microscopy and Raman spectroscopy showed, that the monoclinic crystal structure of α -RuCl₃ is preserved under an homogeneous substitution of Ru by Cr atoms in the whole series, despite an enhancement of stacking disorder under doping [41]. The Ru:Cr ratio of the crystals used for our physical properties measurements was additionally confirmed by energydispersive x-ray spectroscopy (EDX). The oxidation state of Ru and Cr can reasonably be assumed to be 3+ in the whole series like in α -RuCl₃ and CrCl₃. The formation of Cr²⁺ and Ru4+ for particular Cr content values cannot be fully excluded; however, it would lead to a Jahn-Teller distortion, which was not observed in previous x-ray diffraction and Raman spectroscopy experiments [41]. RhCl₃ single crystals were used as a nonmagnetic structural analog compound for the analysis of the specific heat. They were also grown by chemical vapor transport starting from a Rh metal powder and Cl_2 gas in the ratio $n(Cl_2)/n(Rh) = 1.6$ under a temperature gradient from 900°C to 800°C during 6 days. The absence of (magnetic) impurity phases was confirmed.

The dc and ac magnetic susceptibility and specific-heat measurements were conducted with a commercial superconducting quantum interference device magnetometer MPMS-XL and a physical property measurement system by Quantum Design, respectively. For the specific-heat studies a heat-pulse relaxation technique was used. For each measurement of the dc magnetization and the specific heat, the background signal of the sample holder was measured separately and subtracted from the total raw signal.

III. DC MAGNETIZATION MEASUREMENTS

A. Temperature dependence of the magnetization

The temperature dependence of the magnetization up to 30 K of $Ru_{1-x}Cr_xCl_3$ is represented on a log scale in Fig. 2 for a magnetic field $\mu_0H=0.1$ T applied in an arbitrary direction within the *ab* plane and transverse to the *ab* plane [46]. For both field directions the progressive increase on two

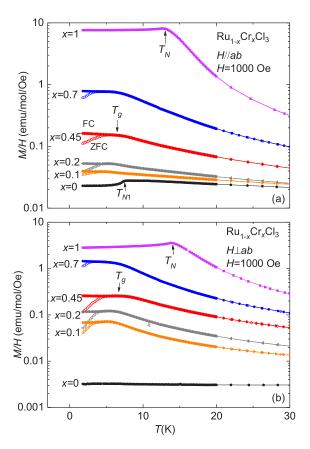


FIG. 2. (a) Magnetization divided by magnetic field M/H of $Ru_{1-x}Cr_xCl_3$ in the ab plane on a logarithmic scale as a function of temperature. No demagnetization correction has been applied. Open and full symbols stand respectively for zero-field-cooled and field-cooled magnetization measurements. The magnetic transition temperatures T_N and T_g are indicated by a change of slope of the magnetization as function of temperature. (b) Same figure but for a transverse field: $H \perp ab$.

orders of magnitude of the low-temperature magnetization with doping suggests the appearance of ferromagnetic interactions between Cr atoms in the basal plane: $J_{\text{Cr-Cr}} < 0$. For doping levels in the range $0.1 \leqslant x \leqslant 0.7$ and for both field directions a phase transition can be observed via a change of slope at $T_g \approx 5$ –7 K followed by a splitting between the zero-field-cooled and field-cooled magnetization curves at low temperature. Finally, the magnetization of CrCl_3 (x = 1) shows an antiferromagnetic transition for both field directions in good agreement with previous magnetization studies on this material [44,47]. This transition is strongly field dependent [44] and its extrapolation to zero field gives $T_N = 13.9$ K for our crystals in agreement with Ref. [44].

The magnetization curves of some $Ru_{1-x}Cr_xCl_3$ single crystals as a function of temperature extending up to 300 K are represented in Fig. 3 for both magnetic fields applied in the basal plane *ab* and transverse to it. For α -RuCl₃ (x=0) the strong magnetic anisotropy previously reported is reproduced [8]. This magnetic anisotropy is a signature of the strong spin-orbit coupling on the Ru site and has mainly been related to the occurrence of off-diagonal Γ magnetic interactions [48].

Following the substitution series to amounts of x = 0.02and x = 0.05 substitution of Ru³⁺ by Cr³⁺, a strong increase of the magnetic susceptibility transverse to the basal plane ab is observed already in the paramagnetic state, without any clear increase of the in-plane magnetic susceptibility. For higher Cr contents $x \ge 0.1$ the magnetic anisotropy gets even reversed on cooling, with a higher magnetic susceptibility transverse to the basal plane at low temperatures $T \leq 15$ K. Such changes of the magnetic anisotropy with temperature are not very common. It was observed in the spin-chain magnet Sr₃NiIrO₆ and explained from the competition between the single-ion anisotropy at the Ni site and anisotropic interactions between Ni and Ir moments [49]. In Ru_{1-x}Cr_xCl₃ the change of the magnetic anisotropy with temperature can probably be attributed to different anisotropies of the magnetization contributions from Ru and Cr moments, see below for a discussion. For an even higher Cr content x = 0.45, the magnetic anisotropy is reversed compared to the one of α -RuCl₃ for the full temperature range, however, collapses at high temperature (T > 150 K). Thus the magnetic anisotropy for x = 0.45 is opposite to the expected anisotropy of the Ru moments given by the Γ interaction on the Ru-Ru links. Finally, for the binary compound $CrCl_3$ (x = 1), a negligible magnetic anisotropy is observed after the consideration of demagnetization effects (see Fig. 3 and Ref. [44]), evidencing the small single-ion anisotropy of Cr moments together with the small anisotropy for Cr-Cr magnetic exchange interactions.

In order to interpret these findings, we now sketch the most likely scenario for the underlying magnetic exchange in $Ru_{1-x}Cr_xCl_3$, focusing on the response in the paramagnetic region. The different couplings K, Γ , J_{Ru-Ru} , J_{Ru-Cr} , and $J_{\text{Cr-Cr}}$ must evolve with doping, since they are sensitive to the bond angles [10]. In the following, we assume that none of these coupling parameters vanishes or changes the sign on substitution $(0 \le x \le 1)$ and the consistency of the data within this assumption will be discussed. First of all, the absence of a clear increase of the in-plane magnetization for small values $x \le 0.05$ indicates an antiferromagnetic nature of the Ru-Cr magnetic exchange interactions. For simplicity, this interaction will be assumed to be of Heisenberg-type. Then, the strong increase of the out-of-plane magnetization under doping must stem from the magnetic moment on the Cr site (S = 3/2), for which an isotropic moment without sizable single-ion anisotropy can be expected. Indeed, while a uniform canting of the Ru moments by an out-of-plane field is suppressed by off-diagonal Γ interactions on Ru-Ru bonds, the Zeeman effect on the Cr sites would be able to overcome the Ru-Cr magnetic interactions thanks to the strong magnetic frustration in Ru_{1-x}Cr_xCl₃. This leads to an out-of-plane alignment of the Cr spins for fields transverse to ab in the paramagnetic regime as schematically depicted in Fig. 4.

In this scenario, the reversed magnetic anisotropy for higher Cr dopings, such as, e.g., x = 0.45, can then be understood by the competition between the different magnetic exchange interactions, which need to be considered in this doping region, i.e., K, Γ , $J_{\rm Ru-Ru}$ on Ru-Ru links, together with an antiferromagnetic $J_{\rm Ru-Cr}$ and ferromagnetic $J_{\rm Cr-Cr}$ on Ru-Cr and Cr-Cr links, respectively (see above). Under

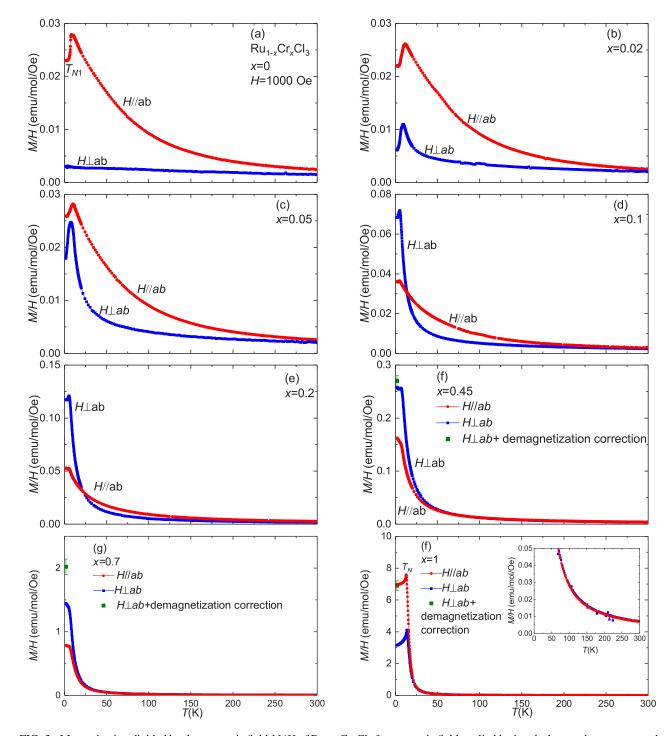


FIG. 3. Magnetization divided by the magnetic field M/H of $Ru_{1-x}Cr_xCl_3$ for magnetic field applied in the ab plane and transverse to the ab plane for (a) x=0, (b) x=0.02, (c) x=0.05, (d) x=0.1, (e) x=0.2, (f) x=0.45, (g) x=0.7, and (h) x=1. The green points at x=1.8 K in (f), (g), and (h) represent the magnetization transverse to the ab plane after correction of the demagnetization effect. This correction was computed from the field dependence of the magnetization represented in Fig. 7 as detailed below. For $CrCl_3$ (x=1) the magnetization at x=1.8 K after correction of the demagnetization effect does not show any anisotropy within the error bars.

magnetic fields applied in the *ab* plane the ferromagnetic Cr-Cr interactions compete with the antiferromagnetic Cr-Ru and the anisotropic Ru-Ru interactions leading to a relatively small increase of the magnetization despite the presence of ferromagnetic interactions. However, under a magnetic field applied transverse to the *ab* plane, the alignment of the Ru moments along the field direction is prevented by the

anisotropic Γ interaction. Thus the Cr spins aligned with the field are less "prone" to existing antiferromagnetic Cr-Ru interactions of Heisenberg type. This effect leads to an opposite magnetic anisotropy for the contribution of the Ru and of the Cr moments to the magnetization. Then, the resulting measured (total) anisotropy is given by the superposition of the two contributions, where the strongest contribution from

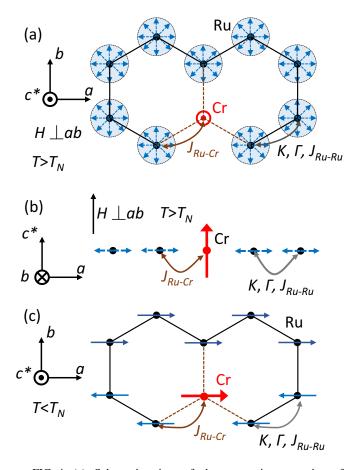


FIG. 4. (a) Schematic view of the magnetic properties of $Ru_{1-x}Cr_xCl_3$ in the low-Cr-content limit $x \ll 1$, in the paramagnetic state $T > T_N$ and under a magnetic field applied perpendicular to the ab plane, i.e., along the c^* axis. The collective alignment of the moments on the Ru site toward the field is prevented by the off-diagonal interaction Γ . As a simplified picture, the moments on the Ru site are represented by blue arrows laying in the basal plane ab. The solid red arrow indicates the spin of the Cr ion, which is polarized by the field transverse to the basal plane. (b) Schematic view from the b axis under the same conditions. (c) Schematic view of the magnetic properties of $Ru_{1-x}Cr_xCl_3$ in the low-Cr-content limit $x \ll 1$ but now in the ordered state $T < T_N$. The red and blue arrows represent the magnetic moments on the Cr and Ru sites, respectively. They are represented in the figure assuming an isotropic antiferromagnetic Ru-Cr interaction. The tilting of the spins out of the basal plane [13] is not represented here for simplicity. The ordering of Ru and Cr magnetic moments explain the reduction of both the magnetic susceptibility in the ab plane and transverse to the ab plane.

Cr moments for x = 0.45 determines the overall magnetic anisotropy of the system.

The evolution of the magnetic anisotropy in the high-temperature limit was mapped out via Curie-Weiss fittings of the magnetization curves in the temperature interval 200 K < T < 300 K, using the equation: $1/\chi = (T - \theta_{\rm CW})/C$ with $C = N\mu_0\mu_{\rm eff}^2/3k_B$. N, μ_0 , and k_B stand for the total number of magnetic ions of Ru and Cr, the vacuum permeability, and the Boltzmann constant, respectively. The effective magnetic moments $\mu_{\rm eff}$ and the Curie-Weiss temper-

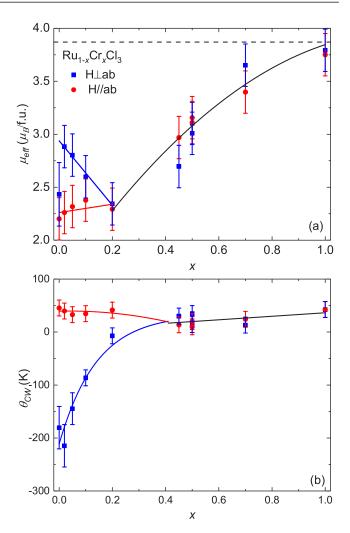


FIG. 5. (a) Averaged effective moment of the magnetic ion Ru/Cr for Ru_{1-x}Cr_xCl₃ as a function of the Cr content x for magnetic fields applied in the ab plane and transverse to the ab plane. Curie-Weiss fits were performed in the temperature interval 200 K < T < 300 K at μ_0H = 1 T. The solid lines are guides to the eye, a single line was drawn above x = 0.2, where the anisotropy of the effective moment is smaller than the resolution of the measurement. The dashed line indicates the free-ion effective moment of Cr³⁺. (b) Fitted Curie-Weiss temperatures for Ru_{1-x}Cr_xCl₃ as a function of the Cr content x for magnetic fields applied in the ab plane and transverse to the ab plane.

atures $\theta_{\rm CW}$ obtained from the fits are represented in Fig. 5 as a function of the Cr content x for both magnetic fields applied parallel and transverse to the ab plane. The average effective magnetic moment is anisotropic below $x \simeq 0.2$: While the effective moment for H//ab is constant within the error bars, the magnetic moment for $H \perp ab$ decreases on the substitution. Above $x \simeq 0.2$, the effective moment is isotropic within the experimental resolution and increases with the Cr content toward $\mu_{\rm eff} = 3.8(1)\mu_B/{\rm f.u.}$ for CrCl₃, which is in agreement with the free-ion effective moment of Cr³⁺ of 3.87 μ_B . The average effective moments of these substitution series are consistent with the assumption of a progressive substitution of Ru³⁺ ions by Cr³⁺ ions without a formation of higher spin ions, i.e., Ru⁴⁺ with S = 1 and Cr²⁺ with S = 2.

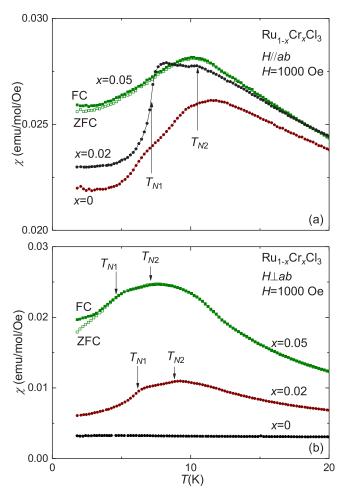


FIG. 6. (a) Low-temperature magnetic susceptibility in the *ab* plane of $Ru_{1-x}Cr_xCl_3$ for the substitution ratios x=0, x=0.02, and x=0.05. T_{N1} and T_{N2} indicate the two successive antiferromagnetic transitions and are determined by the maximum of $d(\chi T)/dT$. (b) Same figure but for a transverse field: $H \perp ab$.

The strong anisotropy of the Curie-Weiss temperature of α -RuCl₃ is a signature of the strong spin-orbit coupling and is related to the occurrence of the off-diagonal magnetic interactions [8,48]. The Curie-Weiss temperature for magnetic fields applied perpendicular to the basal plane decreases in absolute values with the Cr content from $\theta_{\text{CW}} \simeq -200 \text{ K}$ for x = 0 and changes its sign to reach $\theta_{\text{CW}} \simeq 20$ K for x =0.45. The change of behavior of both the effective moment and the Curie Weiss temperature around $x \le 0.2$ suggests, that the contribution from the moment on the Cr sites dominates the magnetization in the high-temperature regime above $x \simeq 0.2$. Thus, the isotropy of μ_{eff} and θ_{CW} for $x \geqslant 0.45$ indicates the absence of strong single-ion anisotropy on the Cr site as well as the existence of dominant isotropic (Heisenberg-type) Cr-Cr magnetic interactions. The magnetic moment on the Ru site has certainly a remaining anisotropy due to anisotropic Ru-Ru interactions for x < 1; however, its contribution is too small to give a sizable anisotropy of μ_{eff} and θ_{CW} within our experimental resolution.

In order to have a closer look at the magnetic ordering in the low-doping region, in Fig. 6 the magnetic susceptibility of Ru_{1-x}Cr_xCl₃ is represented up to 20 K for small substitution ratios x = 0, x = 0.02, and x = 0.05 both for magnetic fields in and transverse to the ab plane. Under magnetic fields in the ab plane the magnetization of α -RuCl₃ (x = 0) shows a sharp transition at $T_{N1} = 7$ K indicating the antiferromagnetic ordering in ABC stacked domains together with a shoulder at $T_{N2} = 10$ K hinting at some domains with stacking faults [13,16]. At x = 0.02 the two magnetic transitions have similar magnitude indicating a strong increase of the stacking disorder under doping in good agreement with previous x-ray diffraction measurements on our single crystals [41]. The magnetic susceptibility for x = 0.05 harbors a single broad transition and shows strong similarities with previous measurements on RuCl₃ powder [12,50] on lower-quality single crystals of α -RuCl₃ [12] or on Ru_{1-x}Ir_xCl₃ single crystals [38]. The tiny splitting between zero-field-cooled and fieldcooled curves below $T \subseteq 3$ K might hint at an incipient weak spin-glass behavior at very low temperatures (see Sec. IV). Thus, the main effect of the substitution of Ru by Cr are an apparent broadening of the magnetic transition(s), likely due to the induced disorder, and a reinforcement of the second magnetic transition T_{N2} with respect to T_{N1} due to an increased amount of stacking faults in the doped samples. A slight downward shift of the two ordering temperatures T_{N1} , T_{N2} indicates the weakening of the zigzag order by the Cr

Under a magnetic field transverse to the ab plane, the magnetic susceptibility of α-RuCl₃ does not show any clear signature of T_N . On the contrary, the magnetic susceptibility transverse to the *ab* plane of $Ru_{1-x}Cr_xCl_3$ for x = 0.02and x = 0.05 show clear signatures of the antiferromagnetic transitions under cooling. Since the magnetic susceptibility transverse to the ab plane appears to be dominated by the magnetic moments on the Cr site (see discussion above), these measurements indicate the freezing of the Cr spins in the antiferromagnetic zigzag state for x = 0.02 and x = 0.05. Under the assumption of an antiferromagnetic Cr-Ru interaction, as explained above, in the zigzag ordered state the Cr moment would point into the opposite direction of its two Ru neighbors on the same zigzag structure/leg, with the antiferromagnetic interaction with the third Ru neighbor not being satisfied. This ordering of Ru and Cr moments is schematically represented in Fig. 4(c).

To conclude, the evolution of the magnetic anisotropy in $Ru_{1-x}Cr_xCl_3$ as a function of the Cr content x is remarkable and can be explained by the competition of a strongly anisotropic Ru-Ru interaction with more isotropic Cr-Cr and Ru-Cr interactions. Overall, our results show, that the anisotropic Γ interactions survive on the Ru-Ru links under partial substitution of Ru by Cr, i.e., when they are diluted on Cr substitution via the reduction of the number of Ru-Ru links in the honeycomb layer.

B. Field dependence of the magnetization

The magnetization of $Ru_{1-x}Cr_xCl_3$ was measured at 1.8 K as a function of the magnetic field applied parallel and transverse to the *ab* plane (see Fig. 7 for our results for x = 0.1, x = 0.45, x = 0.7, and x = 1). Since the $Ru_{1-x}Cr_xCl_3$ single crystals are platelet-like crystals with the a and b axes

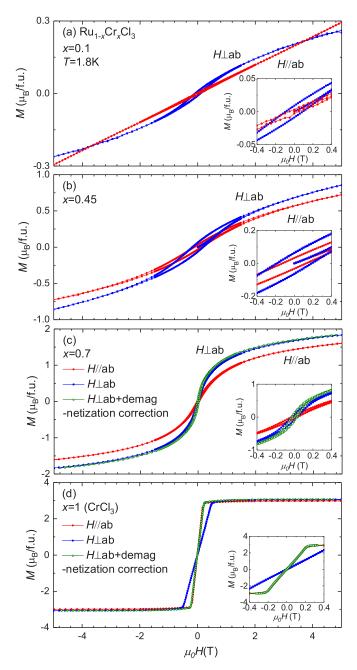


FIG. 7. Hysteresis loop of the magnetization of $Ru_{1-x}Cr_xCl_3$ at T=1.8 K for magnetic field applied in the ab plane and transverse to the ab plane for (a) x=0.1, (b) x=0.45, (c) x=0.7, and (d) x=1. The insets magnify the low-field region. The contribution of the demagnetization effect to the transverse magnetization was evaluated. It is smaller than the symbol size in (a) and (b) and was added to the graph in (c) and (d). For $CrCl_3$ (x=1) the magnetization at T=1.8 K after correction of the demagnetization effect does not show any anisotropy within the error bars.

spanning the plane, the magnetization transverse to the *ab* plane is reduced by the demagnetization effect. The contribution of the demagnetization effect to the magnetization was estimated for all compounds assuming an ellipsoidal shape of the sample from Ref. [51], and was found to be non-negligible for x = 0.7 and x = 1. The demagnetization-corrected mag-

netization transverse to the *ab* plane is also plotted in Fig. 7 for these two compositions.

For x = 0.1, the magnetization shows a clear deviation from the linear behavior expected for an antiferromagnetic state with a hysteresis loop up to 1.3 T for both field directions. It harbors coercive fields of $\mu_0 H_c^{ab} = 0.05 \text{ T}$ and $\mu_0 H_c^{\perp} = 0.09$ T for magnetic fields parallel and transverse to the ab plane, respectively. While the in-plane magnetization is close to a linear behavior in field, suggesting strong antiferromagnetic correlations between the Ru moments, the outof-plane response shows an S-shaped magnetization curve, probably arising from a small static ferromagnetic component from the Cr moments. For x = 0.45, a similar behavior is observed for both field directions, however, with a broadened hysteresis loop and coercive fields of $\mu_0 H_c^{ab} = 0.13 \text{ T}$ and $\mu_0 H_c^{\perp} = 0.19 \text{ T}$. For higher substitution levels, such as for x = 0.7, the hysteresis gets smaller again with a coercive field of $\mu_0 H_c^{ab} = \mu_0 H_c^{\perp} = 0.03$ T. This reduction of the coercive field must come from an interlayer antiferromagnetic Cr-Cr magnetic interaction in addition to the intralayer ferromagnetic Cr-Cr interaction, similarly to the antiferromagnetic interlayer interactions in $CrCl_3$ (see below). For x = 1 hysteresis is absent again indicating the overall antiferromagnetic order at low temperatures in agreement with previous neutron diffraction studies [43]. This ordered state is characterized by a ferromagnetic alignment of the spins within the honeycomb layer and an antiferromagnetic alignment between the layers. After correction of the demagnetization effect, the magnetization of CrCl₃ does not show any magnetic anisotropy within our resolution, confirming the absence of an intrinsic magnetic anisotropy in CrCl₃ as previously proposed in

The full magnetic saturation moment of $Ru_{1-x}Cr_xCl_3$ is expected to increase linearly with the Cr content from $M_{\rm sat} \simeq 1.3~\mu_B/{\rm f.u.}$ for α -RuCl₃ for fields parallel to the *ab* plane [12] to $M_{\rm sat} \approx 3~\mu_B/{\rm f.u}$ for CrCl₃ as observed in Fig. 7(d). Notably, the magnetization 5 T of $Ru_{1-x}Cr_xCl_3$ for Cr concentrations $0.1 \le x \le 0.7$ is still far from the saturation value. This result indicates that the ferromagnetic Heisenberg interactions between Cr atoms coexists with antiferromagnetic interactions and hints further at an antiferromagnetic Ru-Cr interaction within the whole substitution series.

IV. AC MAGNETIC SUSCEPTIBILITY

The ac susceptibility χ_{ac} for some of the $Ru_{1-x}Cr_xCl_3$ single crystals was measured to further elucidate the possibility of a spin-glass state for intermediate substitution values x. The real part of the ac susceptibility χ'_{ac} is shown in Fig. 8 as a function of temperature, measured at a fixed $H_{ac}=5$ Oe transverse to the ab plane, and $H_{dc}=0$ Oe, and at various excitation frequencies f. For low substitution values (x=0.05), the ac susceptibility shows a broad maximum around T=8 K. It is frequency independent within the experimental resolution and follows the dc magnetic susceptibility in Fig. 6(b). This indicates an antiferromagnetic order of Ru and Cr moments broadened by disorder but no spin-glass state. This is confirmed by the imaginary component of the ac susceptibility χ'''_{ac} , which is zero in the full measured temperature regime within the experimental resolution (not

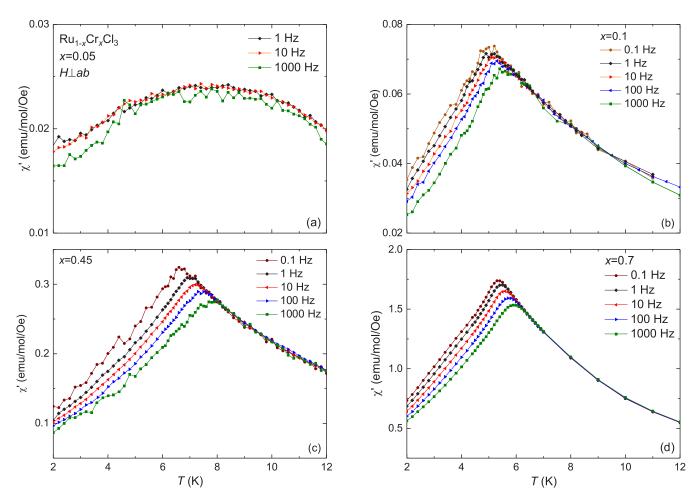


FIG. 8. The real part of the ac susceptibility χ'_{ac} transverse to the *ab* plane as a function of temperature between T=2 K and 12 K at different frequencies for $Ru_{1-x}Cr_xCl_3$ (x=0.05, 0.1, 0.45, 0.7) single crystals.

shown here), as expected for an overall antiferromagnetic structure. Note that, the splitting between zero-field-cooled and field-cooled dc magnetization in Fig. 6 for this sample could already hint at an incipient weak spin-glass behavior for x = 0.05, not resolved in the ac susceptibility in Fig. 8(a).

For the higher substitution levels (x = 0.1, 0.45, 0.7) in $Ru_{1-x}Cr_xCl_3$, the ac susceptibility measurements show clear signatures of a spin-glass transition. A sharp cusp is observed at a transition temperature (T_g) at low frequency (f = 0.1 Hz), and it matches with the freezing temperature observed in the dc (f = 0) susceptibility measurement. The position of this cusp is clearly frequency dependent, a classic signature of a spin-glass transition [52]. With increasing x the freezing temperature $T_g(x)$ displays a maximum around x = 0.45. The observation of a spin-glass state up to at least x = 0.7 indicates, that the magnetic interactions on the remaining Ru-Ru links are still sufficient at x = 0.7 to induce magnetic frustration.

V. HEAT CAPACITY

The specific heat of the $Ru_{1-x}Cr_xCl_3$ series is represented in Fig. 9 as a function of temperature together with the specific heat of the nonmagnetic structural analog compound RhCl₃. It was recently suggested from numerical calculations

of the phonon spectra of α -RuCl₃ and RhCl₃, that the scaling factor for α -RuCl₃ should be adjusted to $\theta_D/\theta_{DRhCl3}=0.92$ [53]. Such a low scaling factor is in contradiction with our experimental results since it would lead to a negative magnetic contribution to the specific heat in α -RuCl₃ above T=15 K. The phonon contribution to the specific heat for Ru_{1-x}Cr_xCl₃ was obtained here by scaling the specific heat of RhCl₃ by the Lindemann correction factor taking into account both the difference in molecular mass and molecular volume between the different compounds [54,55]. Using the unit cell volume measured by x-ray diffraction for each sample, which are published in Ref. [41] for Ru_{1-x}Cr_xCl₃ and V=345.19 Å for RhCl₃, the Lindeman correction factor was estimated to vary with the Cr amount from $\theta_D/\theta_{DRhCl3}=1.00$ for α -RuCl₃ to $\theta_D/\theta_{DRhCl3}=1.14$ for CrCl₃.

The magnetic contribution to the specific heat, $C_{p,\rm mag}$, was obtained by subtracting the estimated phononic contribution from the total measured specific heat. The resulting $C_{p,\rm mag}/T$ of ${\rm Ru}_{1-x}{\rm Cr}_x{\rm Cl}_3$ is represented in Fig. 9(b) as a function of temperature. For x=0 and x=0.02, the specific heat shows the same two transitions T_{N1} and T_{N2} as the magnetization, corresponding to two different stacking sequences, again confirming the predominance of T_{N1} for x=0 and of T_{N2} for x=0.02. Note that the two magnetic transitions are broadened and shifted to lower temperature for Cr-substituted

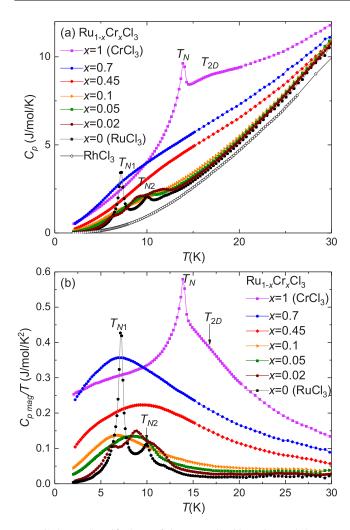


FIG. 9. (a) Specific heat of the $Ru_{1-x}Cr_xCl_3$ series and the non-magnetic analog RhCl₃ as a function of temperature. (b) Magnetic contribution to the specific heat divided by the temperature $C_{p,mag}/T$ as a function of temperature.

x=0.02. For x=0.05 we finally measured a single broad transition. Like for the magnetization, strong similarities can be observed between the specific heat for x=0.05 and previous measurements on RuCl₃ powder [6], on low-quality single crystals of α -RuCl₃ [13] or on Ir-doped single crystals [39]. Thus, this very broad transition for x=0.05 indicates an enhanced disorder inside the layer and in the layer stacking on doping and might lead to a change from a long-range antiferromagnetic zigzag order in α -RuCl₃ to a short-range order in the doped samples. This phenomenon has also been observed in the Ir-substitution series Ru_{1-x}Ir_xCl₃ [39] via a combined specific heat and muon spectroscopy study. This short-range order might already harbor a spin-glass behavior, despite the fact that it could not be clearly resolved in our ac susceptibility measurements.

For higher Cr concentrations, $0.1 \le x \le 0.7$, where the dc and ac magnetic susceptibility clearly indicate a spin-glass state, specific-heat measurements confirm the absence of long-range magnetic order. $C_{p,\text{mag}}/T$ as a function of temperature shows a broad bump with a maximum around T = 7-9 K, i.e., slightly above the spin-glass freezing tem-

perature T_g . This bump indicates an entropy loss via the formation of short-range correlation. Its maximum is at slightly higher temperature for x = 0.45, than for lower Cr content (x = 0.1) or higher Cr content (x = 0.7). An overall increase of the magnetic contribution to the specific heat is observed as function of the Cr content x for $0.05 \le x \le 1$, which is expected for the substitution of $J_{\text{eff}} = 1/2$ by S = 3/2 spins.

For x = 1 (CrCl₃) our specific-heat study further confirms the antiferromagnetic transition at $T_N = 14.1$ K. In addition, a broad bump around $T_{\rm 2D} = 17$ K may indicate the 2D ferromagnetic ordering of CrCl₃ proposed in Ref. [45], although for our crystals this transition is much less pronounced than in a previous specific study on CrCl₃ [44]. Interestingly, our measurements show a significant magnetic contribution to the specific heat in CrCl₃ down to 2 K. This low-T magnetic entropy far below the Néel temperature $T_N = 14.1 \text{ K}$ is likely due to strong fluctuations in this quasi-two-dimensional magnet. At first glance, our results disagree with a previous specific-heat study of CrCl₃ [44], but where the phononic contribution to the specific heat was estimated assuming $C_{p,\text{mag}}/T = 0$ for T < 7.5 K, i.e., a different analysis has been applied. The present study with the use of a nonmagnetic structural analog compound allows to compute the magnetic entropy of CrCl₃ with a higher accuracy, yielding a magnetic entropy $S_{\text{mag}}(30 \text{ K}) - S_{\text{mag}}(2 \text{ K}) = \int_2^{30} C_{p,\text{mag}}/T dT = 8.5 \text{ J/mol/K}$, which is only slightly smaller than the expected value for a S = 3/2 system $(S_{\text{mag,theo}} = R \ln 4 = 11.5)$ J/mol/K).

VI. X-T PHASE DIAGRAM

The experimental results reported in the three previous sections enable us to draw the (x-T) phase diagram of $Ru_{1-x}Cr_xCl_3$ (Fig. 10). The two Néel temperatures T_{N1} and T_{N2} decrease with the Cr content x showing that the Cr S = 3/2 impurities disfavor the antiferromagnetic zigzag order of α -RuCl₃, finally leading to a destabilization of the zigzag order in favor of a spin-glass state for a low-Cr content $x \simeq 0.1$. This spin-glass state is stable for a broad Cr doping interval up to at least x = 0.7, with a maximum of the freezing temperature T_g around $x \leq 0.45$. Due to the proximity of α -RuCl₃ to the Kitaev spin liquid, this spin glass state may harbor bound states of Majorana Fermions as low-energy spin excitations. The transition from the spin-glass state toward the antiferromagnetic order of CrCl₃ in the high-Cr concentration limit could not be investigated in detail in this study due to a lack of suitable crystals. The freezing temperature may evolve continuously toward a second-order magnetic transition on Cr substitution from x = 0.7 to x = 1. A minimum of the freezing/ordering temperature must occur between x = 0.7and x = 1, and the origin and nature of this minimum need to be elucidated in detail in future studies.

VII. SUMMARY AND CONCLUSION

We have studied the magnetic properties of the substitution series $Ru_{1-x}Cr_xCl_3$ by magnetization, ac susceptibility and specific-heat measurements. In the low-substitution limit $x \le 0.05$ the moments on the Cr sites can be considered as magnetic impurities in a Kitaev magnet. These impurities

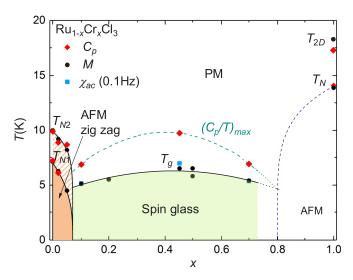


FIG. 10. (x-T) phase diagram of $\mathrm{Ru}_{1-x}\mathrm{Cr}_x\mathrm{Cl}_3$. The black circles, red diamonds, and blue squares are experimental points from magnetization, specific-heat and ac magnetic susceptibility $(f=0.1\ \mathrm{Hz})$ measurements, respectively. The lines are guides to the eye. The orange and the orange and white patterned region corresponds to the fully ordered zigzag state and the region of the phase diagram, where only the part of the sample with numerous stacking faults is magnetically ordered, respectively. The dashed green line indicates the temperature where $dS_{\mathrm{mag}}/dT = C_{p,\mathrm{mag}}/T$ undergoes its maximum. The boundary between the spin-glass state and the antiferromagnetic state on the high-Cr-content side could not precisely be determined in this study and is thus schematically drawn, only.

are antiferromagnetically coupled to the neighboring Ru moments. In an out-of-plane magnetic field, where the response of the Ru moments is small due to the off-diagonal Γ interactions, the Cr impurity moments can easily be tilted because of the small mean field resulting from the frustrated parent state. The unusual evolution of the magnetic anisotropy, showing a reversal of the anisotropy for relatively small x, can be successfully explained via the competition between isotropic Heisenberg and anisotropic magnetic Γ interactions in this series of frustrated magnets. At low temperatures,

the substitution of Ru by Cr results in an evolution of the antiferromagnetic zigzag order into a possible short-range ordered state around $x \simeq 0.05$, and then into a spin glass for $x \simeq 0.1$ indicating that the antiferromagnetic long-range order of α -RuCl₃ is not robust under the substitution of Ru atoms by magnetic Cr impurities. The evolution of the magnetic properties for higher doping levels shows the gradual development from a system dominated by the Kitaev K and off-diagonal Γ interactions toward a system dominated by ferromagnetic Cr-Cr interactions of Heisenberg-type. However, anisotropic Γ interactions on Ru-Ru nearest-neighbor links appear to survive in the whole substitution series. The spin-glass state is observed for a broad Cr content interval up to at least $x \simeq 0.7$ with a maximum of the freezing temperature around x = 0.45.

It should be mentioned that the scenario of isotropic (Heisenberg) Ru-Cr interactions represents a minimal model to explain our experimental observations for the magnetic anisotropy along the series $Ru_{1-x}Cr_xCl_3$. A detailed numerical modeling of susceptibilities is required to resolve possible anisotropies of the Ru-Cr interactions; such studies are currently under way. In addition, a careful characterization of samples at very small doping is called for, in particular also at elevated fields, in order to connect to theoretical investigations of single-impurity effects in the quantum limit and to probe the stability of the proposed field-induced QSL state.

ACKNOWLEDGMENTS

Insightful discussions with E. Andrade, L. Hozoi, L. Janssen, V. Kataev, and S. Nagler as well as technical support by S. Gass is acknowledged. We acknowledge financial support from the DFG through SFB 1143 (Project No. 247310070) and the Würzburg-Dresden Cluster of Excellence on Complexity and Topology in Quantum Matter-ct.qmat (EXC 2147, Project- No. 39085490) as well as from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie Grant No. 796048. K. Mehlawat acknowledges the Hallwachs-Röntgen Postdoc Program of ct.qmat for financial support.

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